

# Act for Your Duties but Maintain Your Rights

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- Autonomy, one of the grand objectives AI
  - Autonomous system, react to environment changes
- Automated strategy synthesis [Pnueli & Rosner, 1989]
  - **Given:** a task expressed in a declarative specification
  - **Obtain:** a strategy (system model)

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- Every nondet. strategy  $\Pi$  captures a set of det. strategies  $\sigma$

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- Duties and Rights
  - Duties: assigned tasks, guaranteed to be accomplished
  - Rights: agent demands, accomplished on the agent's own

# Act for Your Duties But Maintain Your Rights

- Duties and rights,  $LTL_f$  synthesis under environment specifications
  - Tasks in  $LTL_f$  formulas, environment in safety specifications
  - Definition, computational properties, and formally well-founded algorithms
- Further duties and rights, while agent in execution
  - Live synthesis in Formal Methods [Finkbeiner, Klein, & Metzger 2021]
  - Definition, computational properties, and formally well-founded algorithms

# Synthesis with Duties and Rights

## Given:

Environment specification  $env$ , agent duties  $\varphi_d$ ,

## Obtain:

Agent strategy  $\sigma : (2^X)^+ \rightarrow 2^Y$ , a function from past history of environment behaviors to agent actions

$$\forall \gamma \triangleright env, \text{Play}(\sigma, \gamma) \models \varphi_d$$

$\varphi_d$  describes the mandatory goal/task when the environment behaves as its specification  $env$

# Synthesis with Duties and Rights

## Given:

Environment specification  $env$ , agent duties  $\varphi_d$ , agent rights  $\varphi_r$

## Obtain:

Agent strategy  $\sigma : (2^X)^+ \rightarrow 2^Y$ , such that  $\forall \gamma \triangleright env$ ,

- either  $\text{Play}(\sigma, \gamma) \models \varphi_d$
- or  $\text{Play}(\sigma, \gamma) \models \varphi_d \wedge \varphi_r$  if the agent decides to achieve  $\varphi_r$  as well

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The **agent** decides **whether** & **when**

## When: Strategy Enforcing Task wrt History

Environment specification  $env$ , agent task  $\varphi$ , **history**  $h$

Agent strategy  $\sigma : (2^{\mathcal{X}})^+ \rightarrow 2^{\mathcal{Y}}$  enforces  $\varphi$ , with respect to history  $h$ , denoted by  $\sigma \triangleright_h \varphi$

- IF  $\forall \gamma \triangleright env$  such that  $\text{Play}(\sigma, \gamma)$  has  $h$  as a prefix
- THEN  $\text{Play}(\sigma, \gamma) \models \varphi$



# Whether: Strategy Being Right-aware

Environment specification  $env$ , agent duties  $\varphi_d$ , agent rights  $\varphi_r$

Agent strategy  $\sigma : (2^X)^+ \rightarrow 2^Y$  enforcing  $\varphi_d$  is right-aware for  $\varphi_r$ , if  $\forall \gamma \triangleright env$

- $\text{Play}(\sigma, \gamma) \models \varphi_d$
- for every prefix  $h$  of  $\text{Play}(\sigma, \gamma)$ , there exists a strategy  $\sigma_h$  that enforces  $\varphi_d \wedge \varphi_r$  wrt  $h$

# Synthesis With Rights

## Given:

Environment specification  $env$ , agent duties  $\varphi_d$ , agent rights  $\varphi_r$

## Obtain:

Agent strategy  $\sigma : (2^X)^+ \rightarrow 2^Y$  enforcing  $\varphi_d$  that is right-aware of  $\varphi_r$

## Synthesis With Rights: Example

A cleaning robot working in a circular hallway, the charging station is close to the entrance.

**Duty** “cleaning room A”  $\varphi_d = \diamond(\neg Dust\_A \wedge RobotOut\_A)$

**Rights** “fully charging battery”  $\varphi_r = \diamond(BatteryFull)$

1. Take the direction that passes the charging station to room A and clean it. The remaining battery after enforcing  $\varphi_d$  still allows the robot to reach the charging station
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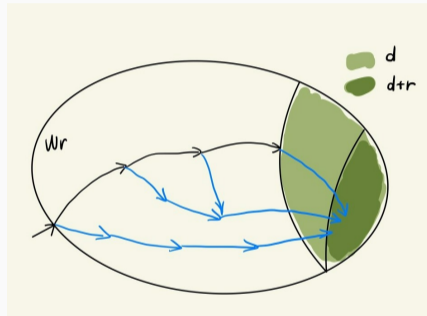
# Synthesis Technique

## Key idea

- **Winning region of reachability game**, maintaining the ability to reach the goal states

## Solution

1. Compute  $W_r$  wrt env. spec.  $env$ , duties  $\varphi_d$  and rights  $\varphi_r$  (2exp time)
  - $A_{env}$  as  $\{\gamma \mid \gamma \triangleright env\}$  [De Giacomo et al. 2021]
  - $A_{env} \times A_{\varphi_d} \times A_{\varphi_r}$ , reachability game
2. **A det. strategy  $\sigma_d$  pursuing  $\varphi_d$**  (black arrows), which **always acts within  $W_r$** 
  - while **achieving  $\varphi_d$**
  - having the **capability of achieving also  $\varphi_r$**



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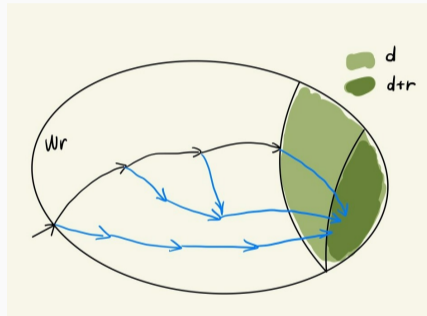
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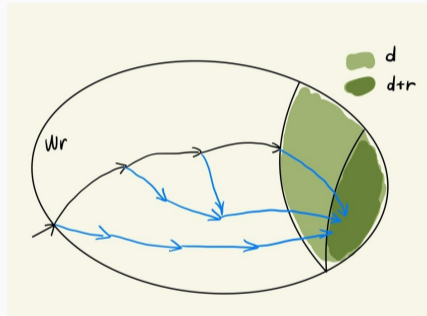
Computationally, linear time



## Achieve rights in execution

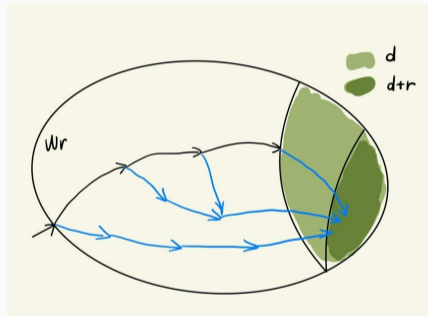
- a nondet. strategy  $\Pi_{d \wedge r}$  pursuing  $\varphi_d \wedge \varphi_r$

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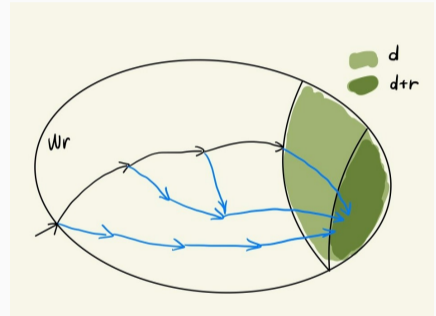
## How does the ultimate strategy work?

- Follow  $\sigma_d$  to achieve duties  $\varphi_d$  (light green zone)
- Choose one strategy from  $\Pi_{d \wedge r}$  to achieve also rights  $\varphi_r$  (dark green zone), **whenever the agent decides to do so**





Computationally, only requires a constant overhead!



## Further Duties and Rights While Executing

- Standard agents
  - Only one task (duty) to accomplish, terminates after finishing
- Intelligent agents
  - Take further tasks (duties and rights) while in execution
  - E.g., a new room to clean while the robot is cleaning the rooms it got assigned at the beginning
- Handling further duties and rights while in execution

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## Synthesis with Further Duties and Rights

**Given:** Environment specification  $env$ , agent duties  $\varphi_d$ , rights  $\varphi_r$ , further duties  $\varphi_{fd}$ , further rights  $\varphi_{fr}$ ,  $h$

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**Obtain:** Agent strategy  $\sigma : (2^X)^+ \rightarrow 2^Y$ , such that

- $\sigma_d$  enforces  $\varphi_d$  and is right-aware for  $\varphi_r$  wrt  $h$
- $\sigma_d$  enforces  $\varphi_{fd}$  and is right-aware for  $\varphi_{fr}$  after  $h$



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The **agent** decides **whether** achieving rights  $(\varphi_r, \varphi_{fr})$  & **when**

## Synthesis With Further Duties: Example

**Duty** “cleaning room A”  $\varphi_d = \diamond(\neg Dust\_A \wedge RobotOut\_A)$

**Rights** “fully charging battery”  $\varphi_r = \diamond(BatteryFull)$

**New duty** “cleaning room B”  $\varphi_{fd} = \diamond(\neg Dust\_B \wedge RobotOut\_B)$

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*Recall:* winning region  $W_r$ , maintaining the ability to achieve  $\varphi_r$

1. Compute  $W_{r \wedge fr}$ , maintaining the ability to achieve  $\varphi_r$  wrt  $h$ , and  $\varphi_{fr}$  after  $h$  (2exp time)

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  - Synchronize the environment with the new duties and new rights!
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Arbitrary subsets of rights: maintain the information and compute on demands



## Conclusions and Future Directions

- Agents handling duties and rights, mandatory tasks and optional tasks
- Further duties and rights arrive in execution
- Multiple duties and multiple rights
  
- More expressive environment specifications
- More expressive task categories, concepts from Deontic Logic